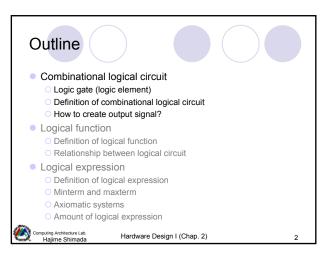
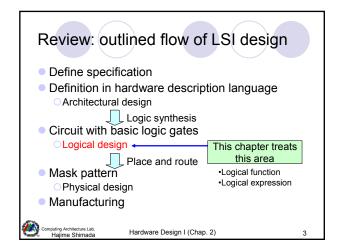
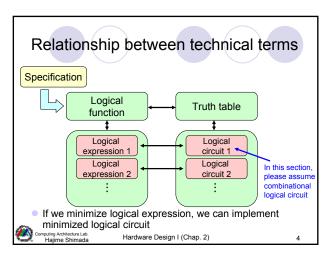
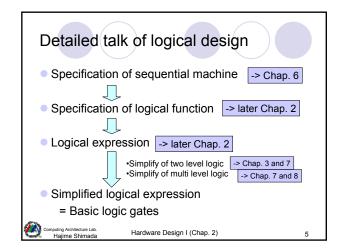
Hardware Design I Chap. 2
Basis of logical circuit, logical
expression, and logical function

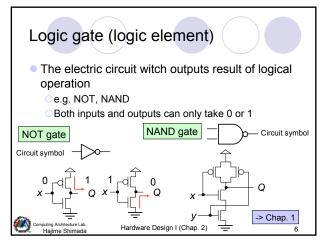
Computing Architecture Lab.
Hajime Shimada
E-mail: shimada@is.naist.jp

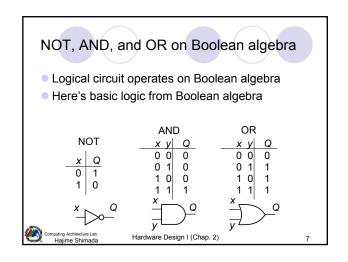


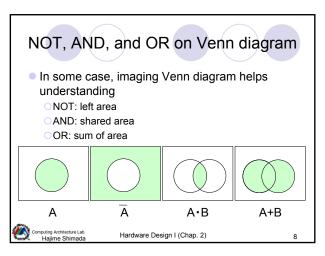


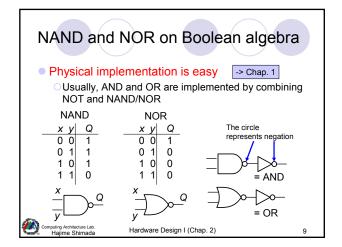


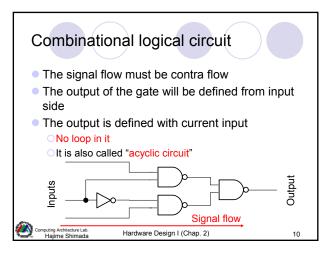


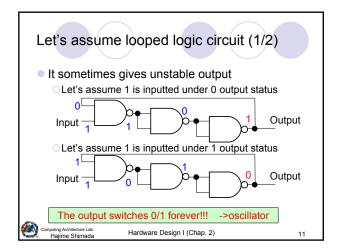


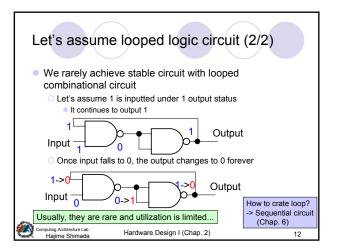




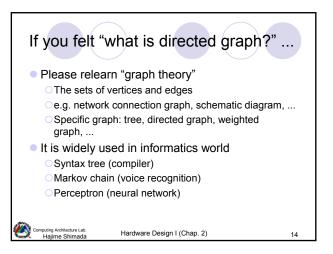


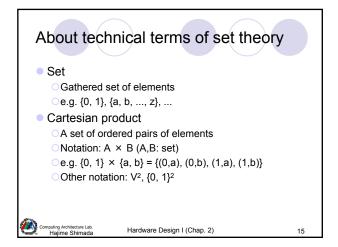


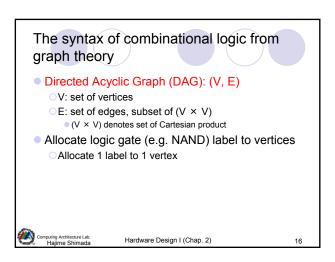


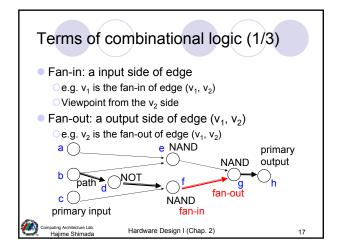


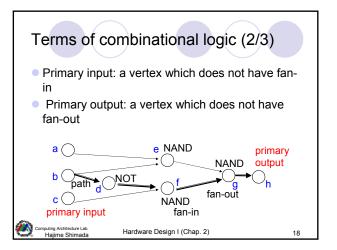
Definition of combinational logic with directed graph Set of vertices: V={a, b, c, d, e, f, g, h} Set of edges: E⊆(V × V) E={(a,e), (b,e), (b,d), (c,f), (d,f), (e,g), (f,g), (g,h)} Label of vertex: NOT, NAND, and so on a e NAND b NAND b NAND hardware Design I (Chap. 2) 13

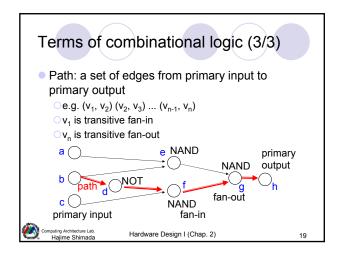


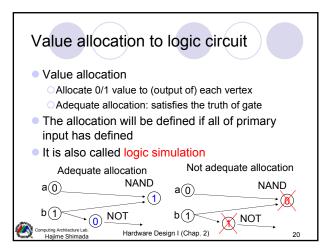


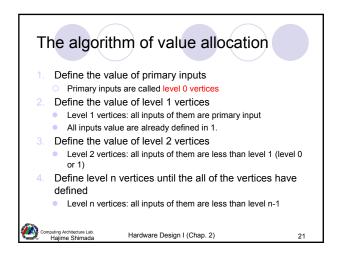


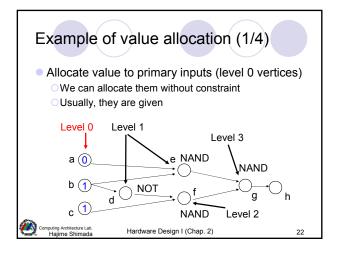


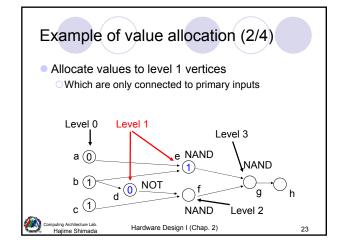


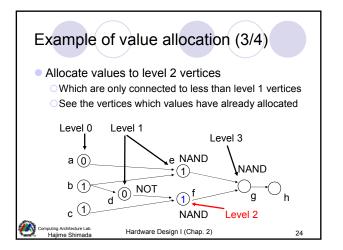


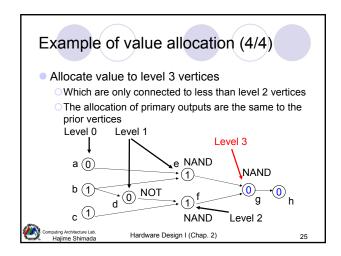


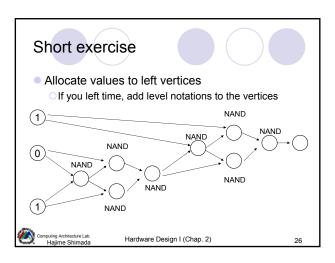


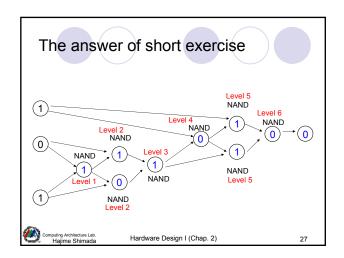


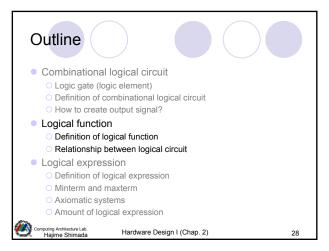


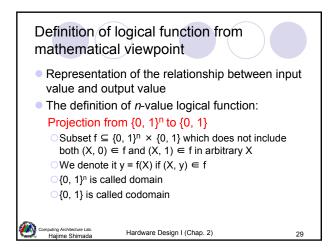


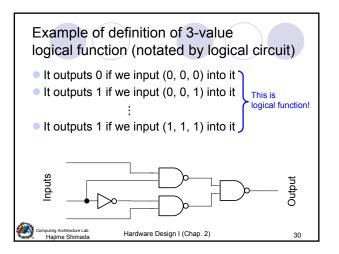


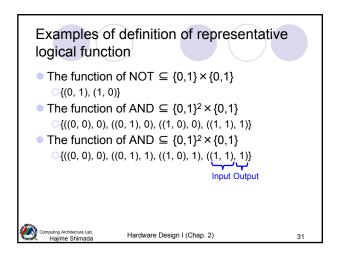


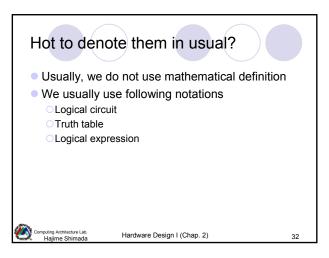


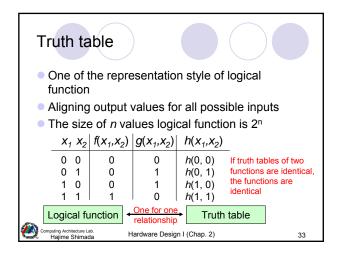


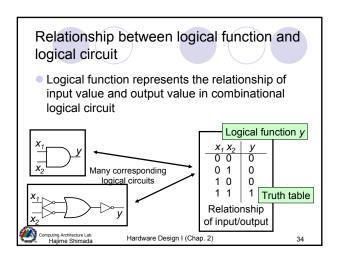


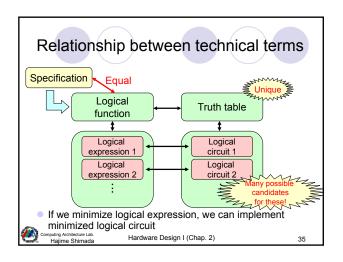


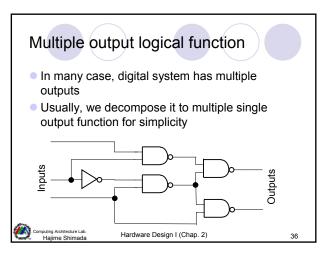












Truth table of multiple output logical function

Multiple output function (*m* outputs):
 Projection from {0, 1}ⁿ to {0, 1}^m

OList of m projections from {0, 1}ⁿ to {0, 1}

$X_1 X_2$	$\int_0^1 f_0(x_1,x_2)$	$f_1(x_1,x_2)$
0 0 0 1 1 0	0 0 0	0 1 1

Computing Architecture Lab.

Hardware Design I (Chap. 2)

Operation between logical functions

 We can extend operation on logical value to logical function

$$(f \cdot g) (x_1, x_2, ..., x_n) = f(x_1, ..., x_n) \cdot g(x_1, ..., x_n)$$

$$(f + g) (x_1, x_2, ..., x_n) = f(x_1, ..., x_n) + g(x_1, ..., x_n)$$

$$(f') (x_1, x_2, ..., x_n) = f(x_1, x_2, ..., x_n)^t$$

Detail is taught in following logical expression section



Hardware Design I (Chap. 2)

Summary of logical function

It is a function from {0, 1}ⁿ to {0, 1}

{0, 1}ⁿ × {0,1} with some constraint

It is represented uniquely with truth table

List of relationship between all inputs and outputs

But it requires 2ⁿ size of memory

We can apply operation on it

Logical function:

The relationship between inputs and outputs

and outputs

Hardware Design I (Chap. 2)

